

# ESc 101: FUNDAMENTALS OF COMPUTING

## Lecture 38

Apr 15, 2010

# OUTLINE

## 1 BINARY TREES

# STORING ELEMENTS IN SORTED ORDER

- In many applications, a large number of elements are stored.
- In many of the operations performed on these elements, it is useful to have the elements in a sorted order.
- Example:
  - ▶ Details of students at IITK: name, roll number, department etc.
  - ▶ For each student, we can have a struct to store all the information.
  - ▶ If these elements are stored sorted by roll number, we can easily find the number of students in a batch for example.

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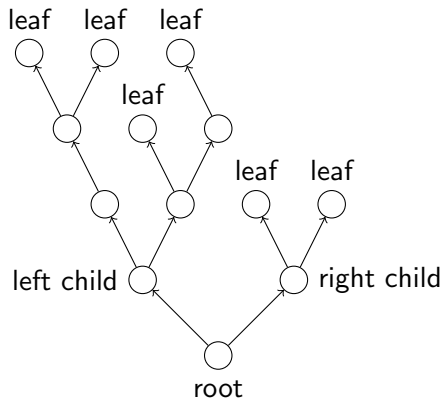
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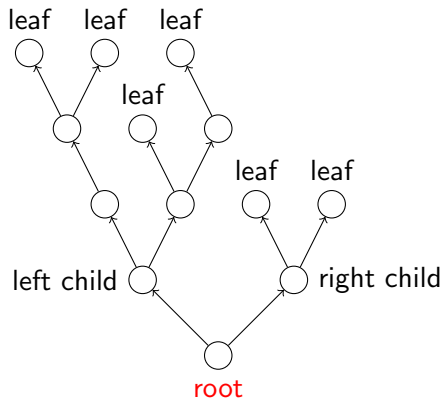
# BINARY TREES

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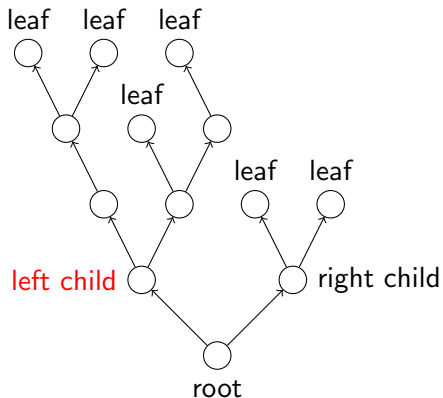
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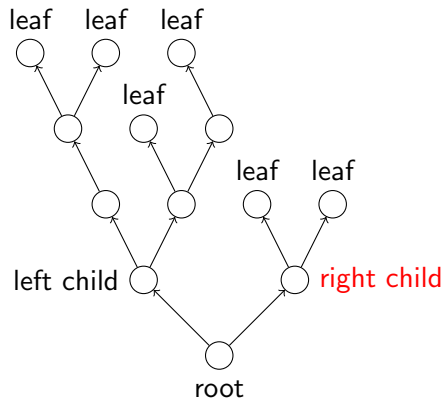
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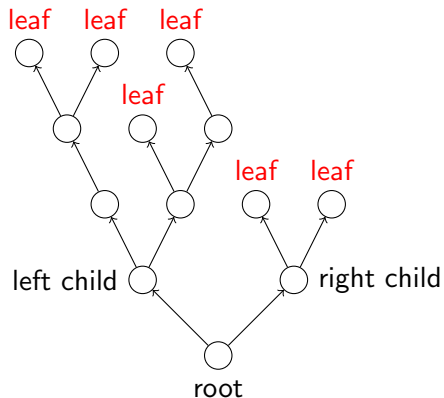
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These are binary trees with the following properties:

- Each node stores an element
- At any node, the element stored is greater than or equal to all elements in the **left subtree** at the node and less than or equal to all elements in the **right subtree** at the node.
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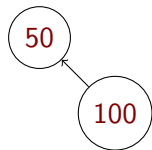
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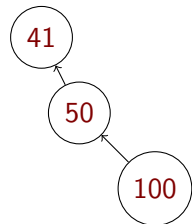
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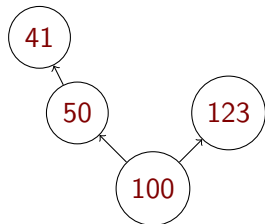


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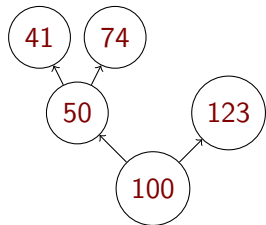




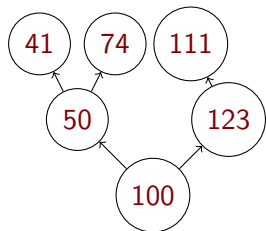
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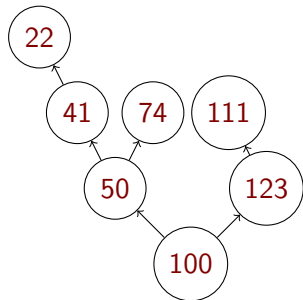
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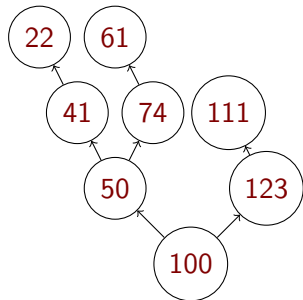
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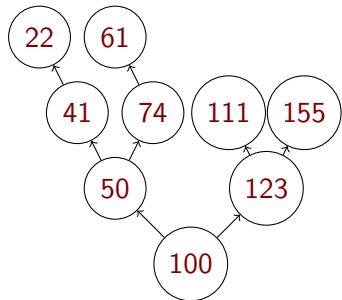
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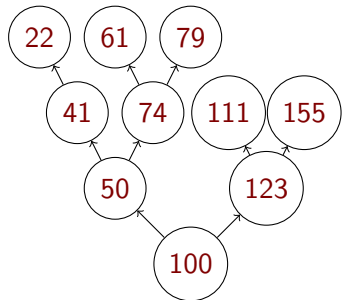
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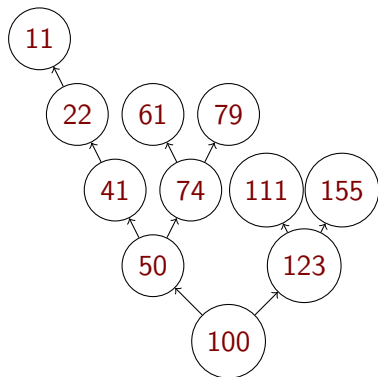
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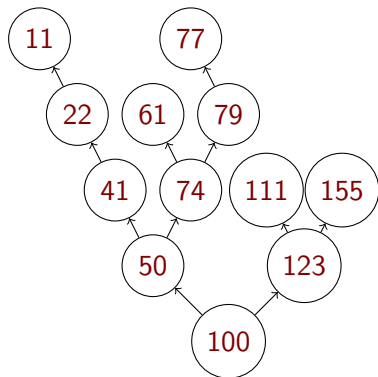


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